Algebra II Curriculum Guide Tier 1 & 2

Unit 2: Building New Function December 1 – January 31



ORANGE PUBLIC SCHOOLS 2018 - 2019 OFFICE OF CURRICULUM AND INSTRUCTION OFFICE OF MATHEMATICS

Algebra II Unit 3 **Contents**

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Overv	new (
Unit	3: Rational Functions and Equations						
Overvi	ew						
This co	ourse uses Agile Mind as its primary resource, which can be accessed at the following URL:						
\checkmark	www.orange.agilemind.com						
Loop	rit consists of 1.2 topics Within cosh topic there are "Evaluring" lossons with concernancing						
Each u	nit consists of 1-3 topics. Within each topic, there are "Exploring" lessons with accompanying						
activity	/ sneets, practice, and assessments. The curriculum guide provides an analysis of teach topic,						
cuggos	tions for pasing, soquence, and emphasis of the content provided						
Sugges	ind Questions						
Essenti							
	How can you transform any given function on the coordinate plane?						
	How do you identify odd and even function based on the symmetry?						
	What is an inverse function?						
	How are a function and its inverse function related?						
	How do you find inverse function algebraically?						
	What is the perent function of a rational function?						
	What is inverse propertien?						
	What is inverse proportion?						
	To simplify the pth root of an expression, what must be true about the expression?						
	How do you solve systems of equations with three variables?						
Enduri	na Understandings						
	A rational function is a function formed by the quotient of two polynomials.						
	Parent function of a rational function is $1/x$						
×	Inverse proportion is when one value decreases at the same rate that the other increases.						
\succ	 You can model a rational function with a table, equation, and graph. 						
\succ	Corresponding to every power there is a root						
\succ	You can combine like radicals using properties of real numbers						
\checkmark	You can write a radical expression in an equivalent form using a fractional (rational) exponent						
	instead of a radical sign						
\succ	Solving a square root equation may require that you square each side of the equation. This						
	process can introduce extraneous solutions						

Common Core State Standards (NJSLS/CCSS)

- 1) A-APR D.6: Rewrite rational expressions 6. Rewrite simple rational expressions in different forms; write a(x)/b(x) in the form q(x) + r(x)/b(x), where a(x), b(x), q(x), and r(x) are polynomials with the degree of r(x) less than the degree of b(x), using inspection, long division, or, for the more complicated examples, a computer algebra system.
- 2) A.APR.D.7: (+) Understand that rational expressions form a system analogous to the rational numbers, closed under addition, subtraction, multiplication, and division by a nonzero rational expression; add, subtract, multiply, and divide rational expressions.
- 3) A-CED A.2: equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.
- 4) F-IF A.1: Understand the concept of a function and use function notation 1. Understand that a function from one set (called the domain) to another set (called the range) assigns to each element of the domain exactly one element of the range. If f is a function and x is an element of its domain, then f(x) denotes the output of f corresponding to the input x. The graph of f is the graph of the equation y = f(x). B. Interpret functions that arise in applications in terms of the context
- 5) F-IF B.4: Interpret functions that arise in applications in terms of the context. For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. Key features include: intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums; symmetries; end behavior; and periodicity.
- 6) **F-IF B.5**: Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes. For example, if the function h(n) gives the number of person-hours it takes to assemble n engines in a factory, then the positive integers would be an appropriate domain for the function.
- 7) F-IF.7b: Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases. b. Graph square root, cube root, and piecewise-defined functions, including step functions and absolute value functions.
- 8) F-BF B.3 Build new functions from existing functions 3. Identify the effect on the graph of replacing f(x) by f(x) + k, k f(x), f(kx), and f(x + k) for specific values of k (both positive and negative); find the value of k given the graphs. Experiment with cases and illustrate an explanation of the effects on the graph using technology. Include recognizing even and odd functions from their graphs and algebraic expressions for them.
- 9) A-CED. A.1: Create equations that describe numbers or relationships 1. Create equations and inequalities in one variable and use them to solve problems. Include equations arising from linear and quadratic functions, and simple rational and exponential functions.
- 10) A-CED.A3: Represent constraints by equations or inequalities, and by systems of equations and/or inequalities, and interpret solutions as viable or non- viable options in a modeling context. For example, represent inequalities describing nutritional and cost constraints on combinations of different foods. Reasoning with Equations and Inequalities

- 11) A-REI A.2: Understand solving equations as a process of reasoning and explain the reasoning 2. Solve simple rational and radical equations in one variable, and give examples showing how extraneous solutions may arise.
- 12) A.RE.D.11. Explain why the x-coordinates of the points where the graphs of the equations y = f(x)and y = g(x) intersect are the solutions of the equation f(x) = g(x); find the solutions approximately, e.g., using technology to graph the functions, make tables of values, or find successive approximations. Include cases where f(x) and/or g(x) are linear, polynomial, rational, absolute value, exponential, and logarithmic functions.

Major Content Supporting Content

Additional Content Parts of standard not contained in this unit Algebra I Content

21st Century Career Ready Practice

- CRP1. Act as a responsible and contributing citizen and employee.
- CRP2. Apply appropriate academic and technical skills.
- CRP3. Attend to personal health and financial well-being.
- CRP4. Communicate clearly and effectively and with reason.
- CRP5. Consider the environmental, social and economic impacts of decisions.
- CRP6. Demonstrate creativity and innovation.
- CRP7. Employ valid and reliable research strategies.
- CRP8. Utilize critical thinking to make sense of problems and persevere in solving them.
- CRP9. Model integrity, ethical leadership and effective management.
- CRP10. Plan education and career paths aligned to personal goals.
- CRP11. Use technology to enhance productivity.

CRP12. Work productively in teams while using cultural global competence.

Algebra II Unit 3 Unit 2: Building New functions (30 Days) Topics:

- Simplifying and solving simple rational functions
- Inverse function
- Transformation of the polynomial
- Even and Odd function
- Radical equation
- Solve Equations with more than two unknowns

Big Rock CCSS	Related Topic	Lesson Objective	Big Rock
			Tasks
 13) P-Br.3. Identify the effect off the graph of replacing f(x) by f(x) + k, k f(x), f(kx), and f(x + k) for specific values of k (both positive and negative); find the value of k given the graphs. Experiment with cases and illustrate an explanation of the effects on the graph using technology. Include recognizing even and odd functions from their graphs and algebraic expressions for them. 14) F.BF.4: Find inverse functions. a. Solve an equation of the form f(x) = c for a simple function f that has an inverse and write an expression for the inverse. For example, f(x) = 2x³ or f(x) = (x+1)/(x-1) for x≠1. c. (+)Read values of an inverse function has an inverse. d. (+) Produce an invertible function by restricting the domain. 	and odd function	 Students will be able to describe transformation for any polynomial represented algebraically or graphically 1.1Bv(F-BF.3) Given a graph or verbal description Students will create the function in the format <i>f</i>(<i>x</i>) + <i>k</i>, and <i>f</i>(<i>x</i> - <i>h</i>) + <i>k</i>, and <i>af</i>(<i>x</i> - <i>h</i>) + <i>k</i>. And create a graph 1.2(F-BF.3) Students will Identify if a polynomial is even or odd graphically and allgebraically 	the Department drobox
		 2.1 (F.BF.4) Students will Understand graphical, tabular, and algebraic relationship between a linear function and its inverse with and without context and find inverse of the linear function 	

Solving systems of equations	 3.1a (A.RE.D.11) Using a graphing calculator Students will Solve systems of equations and interpret solution 3.1b (A-REI.6) Given a linear and quadratic equation students will Solve systems of equations algebraically
	 3.1c (A-REI.6) Given three linear equations students will Solve systems of equation algebraically

Algebra II Unit 3 **Calendar**

December 2018								
Sun	Mon	Tue	Wed	Thu	Fri	Sat		
						1		
2	3	4	5	6	7	8		
9	10	11	12	13	14	15		
16	17	18	19	20	21 Half Day Christmas break starts	22		
23	24 Christmas Eve No School	25 Christmas No School	26 Christmas No School	27 Christmas No School	28 Christmas No School	29		
30	31 New Year's eve No School							

January 2019								
Sun	Mon	Tue	Wed	Thu	Fri	Sat		
		1 New year No School	2	3	4	5		
6	7	8	9	10	11	12		
13	14	15	16	17	18	19		
20	21 MLK No School	22	23	24	25	26		
27	28	29	30 Half Day	31 Half Day				

Algebra II Unit 3 Assessment Framework

Assessment	Assignment Type	Grading	Source	Estimated in-class time	When?
Diagnostic Assessment Unit 3 Diagnostic	Test	Traditional (zero weight)	Curriculum Dept. created – see Dropbox	< ½ block	Beginning of unit
NWEA - Winter	Screener	Graded online	N/A	1 block	End of December
MP 2 Benchmark	Test	Graded on Edulastic and some questions requires Rubric	Curriculum Dept. created – distributed at end of unit	1 block	End of Cycle 2
Performance Task Unit 3 Performance Task1	Authentic Assessment	Rubric	Topic constructed response (also see Dropbox)	½ block	In topic 8
Performance Task Unit 3 Performance Task2	Authentic Assessment	Rubric	Topic constructed response (also see Dropbox)	½ block	In topic 9
Teacher Created Test	Test				
Quizzes	Quiz	Rubric or Traditional	Teacher created or "Practice" in Agile Minds	< ½ block	Varies (must have 3 quizzes per MP)

Algebra II Unit 3 Scope and Sequence

Overview						
Agile Mind Topic	Name	Agile Mind "Blocks"*	Suggesting Pacing			
2	Inverse Function	1	2 days			
3 and	Transformation and even/odd functions	3	5 Days with			
some of 5			supplements			
8	Rational Functions	3	2 to 3 days			
9	Rational Equations	1	2 days with			
			supplements			
10	Square Root Function and Equation	n/a	2 days			

Diagnostic Assessment	½ day
Nwea	1 day
Teacher created Assessment	2 days
MP 2 Benchmark assessment	1 day
Performance Task 1	½ day
Performance Task 2	½ day
Review	1 day
Total	11 days

*1 Agile Mind Block = 45 minutes

Topic 2: Understanding Inverse Relations

Topic Objectives (Note: these are not in 3-part or SMART objective format)

- 1. Understand graphical, tabular, and algebraic relationship between a linear function and its inverse.
- 2. Understand the relationship between exponential and logarithmic functions
- 3.
- 4. Understand the relationship between quadratic and square root functions
- 5. Identify one-to-one functions
- 6. Be able to restrict the domain of a quadratic function in order for its inverse to be a function

Focused Mathematical Practices

- MP 2: Reason abstractly and quantitatively
- MP3: Model with mathematics
- MP 5: Use appropriate tools strategically
- MP 6: Attend to precision
- MP7: Look for and make sense of structure

Vocabulary

 Relation, Inverse function, Quadratic function, Parabola, One to one function, exponential function logarithmic function, discriminant,

Fluency

- Definition of functions and relations
- Determine rate of change from graphs, tables and function rule
- Identify domain and range of a function from graphs and tables
- Determine distance from one point to another point in a Cartesian plane
- Understand different forms of linear and quadratic functions

NOTE: Skip Exploration "Defining parabolas"

	Suggested Topic Structure and Pacing						
Block	Objective(s) covered	Agile Mind "Blocks" (see Professional Support for further lesson details)	МР	Additional Notes			
1	1	Block 1 Block 2	2, 3,8	Cover the guided practice questions aligned to this block			
2	2	Block 3	2, 3, 5,6	This block is kept the same as agile mind so that guided practice can be covered. This topic is not intended to cover square root functions fully but intended to focus on developing the concept of inverse function and identifying parent function			
3	3,4, 5	Block 4, 5,	2, 5, 6, 7	This topic is not intended to cover exponential and logarithmic function fully but intended to focus on developing the concept of inverse function and identifying parent function			

4	Block 6,		Use this block for extra practice and assessment				
			Concepts			Skills	
	CCSS		What students wi	ll know		What students will be able to do	Material/Resource
function find the doma	rom one set (c in) to another e range) assia	called set	 Domain and range function, rate of change fro 	e of a		 Identify domain and range of a function from graph Determine rate of change 	Topic 2: * Overview *Exploring
each elem exactly on	nent of the dor ne element of t	nain the	 Table of change from table and function Understand dependence 	n rule ndent and		from graph, table and an equation	*Exploring "The inverse of a linear function: SAS 2: Q 3-7 SAS 2: 17, 18,
range. If f is an elem then f(x) c	is a function of its dom denotes the ou	and x nain, ntput	 independent varia understand quadr linear function 	ables atic function	n,	• Write linear equation from a table and graph using slope intercept form and point	
input x. Th graph of t f(x)	he graph of is the equation y	the =	 process of solving equation Block 1 New Concept of relation and inverse 			 Determine independent and dependent variables form a table and graph 	19a-c, 20, 21
F.IF.2: Us notation. for inputs	e function Evaluate funct in their doma	tions ins,	 Inverse relation of a lequation using a table The graph of inverse 	linear e and graph	ı	 Identify a quadratic function and linear function Solving two step linear 	
and interp that use fi terms of a	oret statement unction notati a context.	ts on in	 The graph of inverse function is reflection of the graph of the original function across line y=x 		 Solving two step linear Solving two step linear equation with rational coefficients 		
F.IF.5 Relate the domain of a function to its graph and,		in of Ind,				 Solving literal equation Block 1 New Find inverse relation of a 	
quantitati describes.	ive relationshi For example,	p it if				Inear equation using table and equationGraphing inverse relation	
number og	f person-hours	s it				Write inverse function rule	
takes to assemble n engines in a factory, then the positive integers would be an appropriate domain for the function. F.BF.4: Find inverse		be for	Block 2 Review: Exponential equations, Law of exponent, vertical line test			 Block 2 Review Writing exponential equations, Applying Law of exponent 	Agile Mind Topic 2: *Exploring :"
		b inverse Block 2 New: • Concept of Fractal			Apply(PowApply	(Power rule)Apply vertical line test to	The exponential function and
a. Sol	lve an equatio e form f(x) = c	n of for a	 logarithmic function Horizontal line test relation) 	on : (one-to-on	e	determine if the function is a relation	its inverse"
sin ha:	nple function f s an inverse ar	f that nd	 Inverse of an export 	nential		Block 2 New:	
wr for exi	ite anexpressi the inverse. F ample, f(x) =2	on ⁻ or x ³ or	 function as the log function Y = b^x is not one to 	one functio	on	test to determine if the inverse function of a given	
$f(x) = (x+1)/(x-1)$ for $x \neq 1$.		for	when b = 1 • $f^{-}(x)$ notation to $loa_{h}x$	denote y =	=	 function is a function Writing inverse of an exponential function using 	
c.(+)Re inv a g giv	ead values of a verse function graph or a tabl ven that the	n from e,	 Domain and range function of expone 	of inverse ntial functic	on	 Understanding that Y = b^x is not one to one function 	
						when $b = 1$	

function has an inverse. d. (+) Produce an invertible function from a non- invertible function by restricting the domain		 Use f⁻(x) to denote inverse of a function Interpreting domain and range of an inverse exponential function from graph 	
	 Block 3 Review: Various form of quadratic function Domain and range of a quadratic function Square root Horizontal line test on original function Block 3 New: Inverse function of quadratic function 	 Block 2 Review: Identifying domain and range of inverse of a quadratic function from graphs Block 3 New Writing inverse of a quadratic function using table and equation Graphing with restricted domain for the inverse of quadratic to be a function (similar to piecewise function) 	Agile Mind Topic 2: *Exploring: "The quadratic function and its inverse" SAS 4: Q9-11 Q16a-c and Q17
	Block 4 Review: Guided Practice, Constructed Response	<i>Block 4 Review:</i> Guided Practice, Constructed Response	Topic 2 *Guide Practice *Constructed Response (one-to-one computer needed) More Practice P5-8

Topic 3: Transforming functions

Topic Objectives (Note: these are not in 3-part or SMART objective format)

- 1. Apply transformations to graphs of parent functions
- 2. Recognize the general form of a quadratic equations and explains how the values of a, h, and k affects the shape of the parabola
- 3. Describe the transformations from one function to another in terms of vertical shifts, vertical shrink, stretches, and horizontal shifts
- 4. Relate geometric transformations to tables of values for functions
- 5. Identify odd and even functions from equations and graphs

Focused Mathematical Practices

- 6. MP 2: Reason abstractly and quantitatively
- 7. MP 4: Model with mathematics
- 8. MP 5: Use appropriate tools strategically
- 9. MP 6: Attend to precision
- 10. MP 7: Look for and make use of structure

Vocabulary

Transformations of functions, parent function, vertical shift, horizontal shift, vertical stretch, vertical shrink, vertical compressions, quadratic function, Even function, Odd function

Fluency

- 11. The general shape of the graph of a quadratic function
- 12. Plotting points
- 13. Reflecting functions, vertical stretches and shrinks, and vertical shifts of quadratic functions

		Suggested T	opic Struct	ure and Pacing
Block	Objective(s) covered	Agile Mind "Blocks" (see Professional Support for further lesson details)	МР	Additional Notes
1	1 - 2	Block 1 Block 2	2,4	
2	2 - 3	Block 3 Block 4	2, 4, 5,7	Provide computers for students to explore the effect of a, h, and k in a quadratic function (at least 1 computer for each group)
3	4	Block 5	4, 5 7	
4	1-4	Block 6 and 7		Have students correct the problems they got incorrect on the Guided practice, showing all work.

CCSS	Concepts What students will know	Skills What students will be able to do	Material/Resource
 F.BF.3: Identify the effect on the graph of replacing f(x) by f(x) + k, k f(x), f(kx), and f(x + k) for specific values of k (both positive and negative); find the value of k given the graphs. Experiment with cases and illustrate an explanation of the effects on the graph using technology. Include 	 Block 1 Review: Parent function of linear and quadratic functions expressions with negative exponents Translation, Reflection Block 1 New Family of parent functions Absolute value function Transformation to fit the data 	 Block 1 Review Evaluate expressions with negative exponents Translating linear and quadratic functions vertically and horizontally Block 1 New Define Parent function and transformation Identify Family of parent functions Identify Absolute value function 	Agile Mind Topic 3: *Overview *Exploring "Transformation s to fit data" P1- 7 SAS 1: Q4a-c Q9z-b Q1-a-b More practice P 1-3
technology. Include recognizing even and odd functions from their graphs and algebraic expressions for them.	 Block 2 Review: Vertex form of the quadratic equation Y= A(x-h)² + k simple quadratic equation y= (x² + k) Block 2 New: Effect of a, h, and k Piecewise function 	 Block 2 Review: Identify Vertex form of the quadratic equation A(x-h)² + k Describe Effect of K on simple quadratic equation y= x² + k Block 2 New: Describe the Effect of stretch factor, horizontal shift and Vertical shift Transform Piecewise function 	Agile Mind Topic 3: *Exploring "Transformation s to fit data" P 8-13 *Exploring "Generalizing transformation" SAS 2: Q16 Q18a-c SAS 3: Q8, 9 & Q10a-b ** Computers for at least 1 for each group
	 Block 3 Review: Evaluating algebraic expressions Block 3 New: Algebra and geometry connection 	 Block 3 Review: Evaluating algebraic expressions with negative integers Block 3 New: Making Algebra and geometry connection to determine the effect of horizontal shift Decide algebraic rules for function transformation 	Agile Mind Topic 3: *Exploring: "Making the algebra- geometry connection" *Summary SAS 4: Q6-9

 Block 4 Review Rotation, Reflection Block 4 New Definition of even and odd functions Definition of Line symmetry Point symmetry 	 Rotating shapes on a coordinate plane Reflecting lines over line <i>New</i> Sketching graphs given intervals where the function is concave up or down and given the point of inflection Determining whether a function is even or odd graphically Determining whether a function is odd or even algebraically 	Day 4 (Material) Agile Mind Topic 4 * Exploring "Quadratic and Cubic" P10 - 11 SAS 3 Q15a - c GP 7 - 10 MP pg. only 11 Department provide supplements for identifying even	
Block 5 : Guided Practice, Constructed Response		algebraically, graphically Agile Mind: *Guided Practice *Constructed response Moe practice: P 4-11 ** Computer provided for each student	

Topic 8: Rational functions

Topic Objectives (Note: these are not in 3-part or SMART objective format)

- 1. Define rational function and create rational functions.
- 2. Interpret models of rational functions.
- 3. Demonstrate transformation of functions on rational functions using parameter changes.

Focused Mathematical Practices

- MP 2: Reason abstractly and quantitatively
- MP4: Model with mathematics
- MP 5: Use appropriate tools strategically
- MP 6: Attend to precision
- MP7: Look for and make sense of structure

Vocabulary

Rational functions, Parent function, Domain, Range.

Fluency

- Computing with percent
- Rates and Ratios
- Writing linear functions with one variables
- Domain and Range

		Sugge	ested Topic Structure	and Pacing
day	Objective(s) covered	Agile Mind "Blocks" (see Professional Support for further lesson details)	МР	Additional Notes
Day 1	1 & 2	Block 1 & 2	2,4,7	Overview: "Rational Function" Pages 1 - 4 Explore: "Modeling with rational functions" page 1 – 5 Department will provide supplements
Day 2	1 & 2 & 3	Block 3 & 4	2, 4, 7	Explore: "Modeling with rational functions" pages 6 – 12

	CCSS Concepts What students will know		,	Skills What students will be able to do	Material/Resource		
1) A-1 Croine an pro arright qui sin qui sin qui sin exit fr 10 F-1 11 fr 11 fc 11 fc 11 gui 12 gui 13 gui 14 gui 15 gui 16 gui 17 gui 18 gui 19 gui 1	CED A.1: eate equations equalities in on- d use them to so oblems. <i>Include</i> <i>sing from linea</i> <i>adratic function</i> <i>adratic function</i> <i>ages and illustration</i> <i>apples. Experime</i> <i>ases and illustration</i> <i>apples. Experime</i> <i>ases and illustration</i> <i>apples. and algeb</i> <i>apples. and algeb</i> <i>appressions for the</i>	and e variable solve e equations or and ins, and ins, and ind ins. ew functions nctions 3. ct on the ng f(x) by f(x) and f(x + k) es of k (both inative); find ven the ent with ate an ne effects on technology. ing even and om their oraic them.	Day 1 Review • Definition of rates ratio, Definition of linear parent function New • Definition of Rational function • Definition of vertical asymptote			 ay 1 Review Writing rates and ratios lew Create rational function Transform rational functions Identify vertical asymptote 	Day 1 Agile Mind Topic 8 * Overview P 1 - 4 * Exploring "Modeling with rational function" P 1 - 5 Suggested assignment: SAS 1 Q7 a - b and 8a - c Guided Practice page 1-5
1) 	BF B.3 Build n from existing fu dentify the effe graph of replaci k, k f(x), f(kx), for specific value oositive and ne the value of k g graphs. Experin cases and illustre explanation of the graph using nclude recogni and odd function graphs and alge expressions for	new functions anctions 3. ect on the ing $f(x)$ by $f(x)$ and $f(x + k)$ ness of k (both gative); find iven the nent with rate an the effects on the effects on technology. zing even ons from their ebraic	Day 2 (ca Review • Concep • Definiti range New • Rationa • Definit rationa	oncept) of of mixtures of of part to whole on of domain & al function ion of the parent Il function		 by 2 (skills)Review Writing ratios with part to whole Transformation with any function Writing ration function for a mixture 	Day 2 (Material) Agile Mind Topic 8 * Exploring *Modeling with rational functions" P 6– 12 More Practice page 1-2 Suggested assignment: SAS 2 Q8 and 9a – c
2) t r ł	wo or more va epresent relation	riables to ionships ities; graph					

Algeb	ra II Unit 3						
	equations on axes with labe	coordinate els and scales.					
			Τ	opic 9: Ra	ationa	Equation	
Topic 1 2 3 Focus	Topic 9: Kational Equation Topic Objectives (Note: these are not in 3-part or SMART objective format) 1. write rational equations to model problem situation 2. Solve rational equations using graphs, tables, and analytic strategies 3. Identify extraneous solutions. Focused Mathematical Practices • MP 2: Reason abstractly and quantitatively • MP4: Model with mathematics						
Vocal Fluen • •	 MP7: Look for and make sense of structure Vocabulary: Rational Equations, Extraneous solutions Fluency Solving proportion Solving linear equations with variables on both sides of the equal sign Creating linear equations with one variable Computing rates in terms of distance and time 						
	Suggested Topic Structure and Pacing						
Day	Objective(s) covered	Agile Mind "Blo (see Professional S for further lesson of	cks" upport details)	МР		Additional Notes	
1	1, 2	Block 2		2, 4, 7	Explor Pages	ing "Solution Methods" 5 – 11	
	CCS	S	Wha	Concepts t students will	know	Skills What students will be able to do	Material/Resource
 A-REI A.2: Understand solving equations as a process of reasoning and explain the reasoning 2. Solve simple rational and radical equations in one variable, and give examples showing how extraneous solutions may arise. A-CED. A.1: Create equations and inequalities in one variable and use them to solve problems. Include equations arising from linear and quadratic functions, and simple rational and exponential functions. Day1 (Concept) Review: Definition of rates Definition of rates Definition of rational equations Definition of rational equations Definition of rational equations Definition of rational equations Definition of extraneous solution 		itional ution	 Day 1 (Skills) Review Computing rates using distance and time Solving equations with variables on both ides Writing proportions Solving proportions New Creating rational equations Solving rational equations 	Day 1 (Material) Agile Mind Topic 9 * Exploring "Rational Equations" P 6-11 SAS 2 Suggested assignment: SAS 2 Q19a-c More Practice 1			

Topic 10: Square root functions and Equation

Topic Objectives (Note: these are not in 3-part or SMART objective format)

After completing the topic square root functions and equations, students will be able to .

- 1. Determine the reasonable domain and range values of square root functions when given in context, as well as interpret and determine the reasonableness of solutions to square root equations.
- 2. Analyze situations modeled by square root functions
- 3. Formulate equations, select a method and solve problems
- 4. Relate representations of square root functions, such as algebraic, tabular, graphical and verbal descriptions
- 5. Solve square root equations

Focused Mathematical Practices

- MP 2: Reason abstractly and quantitatively
- MP 4: Model with mathematics
- MP 5: Use appropriate tools strategically
- MP 6: Attend to precision
- MP 7: Look for and make use of structure

Vocabulary

Quadratic formula, Imaginary numbers, complex numbers, discriminant, real roots and complex roots

Fluency

- Order of Operations
- Creating and analyzing graphs and tables
- Domain and range
- Transformation of functions
- Inverting a functional relationship
- Simplifying radical expressions

Day Objective(s) covered Agile Mind "Blocks" (see Professional Spport for further lesson details) MP Additional N	lotes
1 all Block 1 2,4,5 Supplement in dropbox(see in the see in the second s	ne 16-17 Tier 1 Unit 3)

	CCSS	CCSS Concepts What students will know		Material/Resource
1)	F-BF B.3 Build new functions from existing functions 3. Identify the effect on the graph of replacing $f(x)$ by $f(x) +$ k, k $f(x)$, $f(kx)$, and $f(x + k)$ for specific values of k (both positive and negative); find the value of k given the graphs. Experiment with cases and illustrate an explanation of the effects on the graph using technology. Include recognizing even and odd functions from their graphs and algebraic expressions for them. A-REI A.2: Understand solving equations as a process of reasoning and explain the reasoning 2. Solve simple rational and radical equations in one variable, and give examples showing how extraneous solutions may arise. A.RE.D.11. Explain why the x- coordinates of the points where the graphs of the equations $y = f(x)$ and $y = g(x)$ intersect are the solutions of the equation $f(x) = g(x)$; find the solutions approximately, e.g., using technology to graph the functions, make tables of values, or find successive approximations. Include cases where $f(x)$ and/or $g(x)$ are linear, polynomial, rational, absolute value, exponential, and logarithmic functions.	 Day1 (Concept) Review Definition of parent functions Effect on the graph of f(x+k), f(x)+k, kf(x), f(for the parent function f(x) Domain and Range New Definition of square function Transforming the sq root functions require the same concept as other parent functio Domain and range is the Square root pare function 	Day 1 (Skills) Review• Identifying parent linear, quadratic, exponential and logarithmic function• Determine domain and range of any function• Determine domain and range of any function• Determine domain and range of any function• Identifying square root function• Identifying square root function• Identifying square root function• Identifying square root function• Identify Domain and Range of Transformed Square root equations• Solve square root equations	Day 1 (Material) Dropbox Tier 1 Unit 3

Ideal Math Block

The following outline is the department approved ideal math block for grades 9-12.

- 1) Do Now (7-10 min)
 - a. Serves as review from last class' or of prerequisite material
 - b. Provides multiple entry points so that it is accessible by all students and quickly scaffolds up
- 2) Starter/Task (10 to 15 min)
 - a. Designed to introduce the lesson
 - b. Uses concrete or pictorial examples
 - c. Attempts to bridge the gap between grade level deficits and rigorous, on grade level content
 - d. Provides multiple entry points so that it is accessible by all students and quickly scaffolds up
- 3) Mini-Lesson (15-20 min)
 - a. Design varies based on content
 - b. May include an investigative approach, direct instruction approach, whole class discussion led approach, etc.
 - c. Includes CFU's
 - d. Anticipates misconceptions and addresses common mistakes
- 4) Class Activity (25-30 min)
 - a. Design varies based on content
 - b. May include partner work, group work/project, experiments, investigations, game based activities, etc.
- 5) Independent Practice (7-10 min)
 - a. Provides students an opportunity to work/think independently
- 6) Closure (5-10 min)
 - a. Connects lesson/activities to big ideas
 - b. Allows students to reflect and summarize what they have learned
 - c. May occur after the activity or independent practice depending on the content and objective
- 7) DOL (5 min)
 - a. Exit slip

Algebra II Unit 3 MTSS MODEL

Whole Group Instruction	50 min	INSTRUCTION (Grades 9 – 12) TOOLS Daily Routine: TOOLS Mathematical Content or Language Routine Manipul Anchor Task: Anticipate, Monitor, Select, Sequence, Connect RESOU Agile M Collaborative Work* Guided Practice Independent Work (Demonstration of Student Thinking) Independent Work (Demonstration of Student Thinking)			atives RCES ind
Rotation Stations (Student Notebooks & Chromebooks Needed)	1-2X 25 min	STATION 1: Focus on current Grade Level Content STUDENT EXPLORATION* Independent or groups of 2-3 Emphasis on MP's 3, 6 (Reasoning and Precision) And MP's 1 & 4 (Problem Solving and Application) TOOLS/RESOURCES Agile Mind Math Journals	STATION 2: Focus on Student Need TECH STATION Independent TOOL S/ RESOURCE Khan Academy Approved Digital Prov Fluency Practice	ds S ider	TEACHER STATION: Focus on Grade Level Content; heavily scaffolded to connect deficiencies TARGETED INSTRUCTION 4 – 5 Students TOOLS/ RESOURCES Agile Homework Manipulatives
	5 min	INSTRUCTION Exit Ticket (Demonstration of Stud TOOLS/RESOURCES Notebooks or Exit Ticket Slips	ent Thinking)		

Algebra II Unit 3 Sample Lesson Plan (Agile Mind)

Lesson	Topic 8 Rational Functions Exploring "Modeling with Rational Functions"	Days	1
Objective	By using the concept of a quiz grade SWBAT	CCSS	A.CED.A1
	Define rational function and create rational		
	functions.		
	Interpret models of rational functions.		
Learning	Materials needed: Computer with projection device, tran	sparency	to insert the activity sheets,
activities/strategies	and activity sheets		
	Fluency Practice: (5 minutes) A builder could get 6 sheet	s of sheetr	ock for \$9. If he bought 12
	sheets, how much money would he have spent?		
	Do Now (5 minutes): If you scored 16/25, 20/25, 10/25, a	and 18/25	on 4 different quizzes in
	your math class, What must you score on the 5 th quiz in c	order to ac	hieve an average grade of
	Starter/Launch (3 minutes):		
	Students will work on the distance verses time ta	ble on the	student activity sheet
	problem 1. After they complete the table ask stu	dents the	following questions
	What kind function is this?		
	What is the appropriate domain for this context? Discuss the sharactoristics about the graph to provent it if	rom hoin	a over a nontial or
	Discuss the characteristics about the graph to prevent it i	rom being	g exponential of
	Mini lesson and practice (20 minutes):		
	Note: Every bullets need to be timed.		
	 Display page 1 from "Overview" and ask students (Two different way) 	s how can	they write 3/20 as percent
	 Show page 2 and give students time to find the g 	rade after	the second quiz. [SAS 1.
	question 2] Play panel 1 as needed to check stud	ent work.	
	Advance to panel 2 of the animation and give stu	dents time	e to make sense of the
	table shown there. Be sure students understand	that the tv	wo additional numbers in
	the first column of the table reflect the cumulativ	e points e	earned after the third and
	auestion 3al	inplete 3P	is I question sa [SAS I,
	 If needed, play panel 2 to allow students to check 	k their ent	ries. Then, give students
	time to write a function that models the data in t	he table, a	as prompted in the final
	caption. [SAS 1, question 3b] Use these questions	s if studen	ts appear to be struggling:
	What was staying constant or same in the	ne process	s column?
	What was varying or changing?		
	 Use panel 3 as needed to confirm students' funct What does the final grade depends on? 	ion rules.	Ask student:
	Ask students to graph the function and determin	e the num	ber of additional points
	needed for a grade of 90% [SAS 1, question 4]. To	confirm t	heir answer show students
	Page 3 and ask a student to come up to the smar	t board to	move the slider
	(animation) to verify their answer	المراجع والمراجع	an late at a dant a stirite :
	 Snow page 4 to define rational function. Have stu sheet 1 questions 5 and 6 	idents cor	inplete student activity

*	
	Have students do a Read Pair Share of the text on page 4. (Read by themselves, then pair up with someone and share what they read and if there is anything they didn't understand) Ask students based on the example if they can give some examples of rational
	functions
	• Have students discuss the similarities and differences between Terrence's graph and the graph on page 4. Encourage them to describe any transformations of the parent function they see in Terrence's graph.
	Group work/ Partner work (25 minutes) Show students page 1. Students can individually read the paragraph about building brick wall
	then pair up with a partner and complete the questions $1 - 6$ from the SAS 2 Debrief question 4, 5, and 6 as a class for 5 minutes
	Independent Practice (12 minutes):
	Re-inforce SAS 2 Question 9
	Debrief and check for 2 minutes
	Closure (2 minutes):
	 Ask what is a rational function? How can you model a rational function? What is the parent rational function? What is domain and range of a rational function? And what are some example of rational functions in real life.
	DOL (5 minutes):

Algebra II Unit 3 Supplement Materials

		Tas	ks
CCSS	SMP	Dropbox location and filename	Link (original task and answer key)
		9-12 Dropbox> curriculum algebra	
		2>Tier1/2 > Unit 1 > Performance	
		Assessment> Task1	

ELL/SWD supplement link

<u>http://nlvm.usu.edu/en/nav/vlibrary.html</u> <u>http://www.explorelearning.com/index.cfm?method=cResource.dspBrowseCorrelations&v=s&id=USA-000</u> <u>http://www.thinkingblocks.com/</u>

		Multiple Representations
Linear function	Real Life Image	An airplane flies at a constant Altitude (height vs. time)
		Shows Height of the plants Vs. Time.
	Pictorial	Geometrically f^{-1} is the reflection of f across the line $y = x$. Conceptually, using the <i>box</i> analogy, a function's inverse box <i>undoes</i> what the function's regular box does.
	Plotorial (Coordinate Plane)	Onits Sold 80000 Demand 60000 Curve 50000 Distance 40000 200 90000 y=55x+20 (3, 185)
		20000 10000 Cost (\$) 0 100 200 300 400 0 1 2 3 4 5 Time (hours)





Rational function			
Verbal description	A <i>rational function</i> is a function formed by the quotient of		
Function form	$f(x) = \frac{a(x)}{b(x)}$ where $a(x)$ and $b(x)$ are polynomial functions		
Parent function (Graph)	$f(x) = \frac{1}{x}$		
Parent function (Table)	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		
Function Characteristics	Domain: $\{x \mid x < 0\} \cup \{x \mid x > 0\}$ Range: $\{f(x) \mid f(x) < 0\} \cup \{f(x) \mid f(x) > 0\}$ Zeros: none x-intercept & y-intercept: none Decreasing: $\{x \mid -\infty < x < 0\} \cup \{x \mid 0 < x < \infty\}$ End Behavior: As x approaches - ∞ , $f(x)$ approaches 0; as x approaches + ∞ , $f(x)$ approaches 0. Asymptotes: $x = 0$, $y = 0$		

	Rational equation
Verbal description	Equation that contains rational expressions
Equation	$\frac{Distance}{Distance} + \frac{Distance}{Distance} = Time$
	Rate Rate
Extraneous solution	Extraneous solution is a solution of an equation derived from an
	original equation that is not a solution of the original equation. When
	you solve a rational equation or square root equation, it is possible to
	get extraneous solutions. These values must be eliminated from the
	solution set. Always check solutions by substituting them into the
	original equation
Real life example	Jill takes 2 hours to plant 500 flower bulbs. Jack takes 3 hours to
-	plant 450 flower bulbs. Working together, how long should it take
	them to plant 1500 bulbs
	work = 1500
	$r = \frac{work}{time} = \frac{1000}{time}$
	$\frac{500 flowers}{200 rlowers} + \frac{450 flowers}{200 rlowers} = \frac{1500}{100}$
	2 hr. 3 hr. t
	$\frac{2400}{6} = \frac{1500}{5}$
	6 T
	t = 3.75 hr.
	Square root function and Equation
Parent function	$f(x) = \sqrt{x}$
Transformed function	$f(x) = a\sqrt{x-h} + k$
Graph of the parent	4
function	
	2
	1.
	0
	-4 -3 -2 -1 0 1 2 3 4
	2.

Table of the parent	x	y	
function	0	0	
	1	1	
	2	5	
	3	~12	
	4	2	
	5		
		42	
Characteristics	Domain [.] {	x x > 0	
	Range: {f(x) f(x) > 0	}
	Zeros: x=0)	
	x-intercept: (0, 0) y-intercept: (0, 0)		
	Increasing/Decreasing : Increasing on $\{x 0 < x < \infty\}$		
	End Beha	vior:	
	As x appro	baches + \propto	p , f(x) approaches + ∞ .
Post World Application	The spee	d of a ta	mamilies a function of accord donth:
	The spee		anami is a function of ocean depth.
	SPEED = $\sqrt{d \cdot g}$		
	g = acceleration due to gravity (9.81 m/s ²)		
	<i>d</i> = depth of the ocean in meters		
Understanding the warnings to coastal predict when the ts		nding the to coast when the t	e speed of tsunamis is useful in issuing al regions. Knowing the speed can help tsunami will arrive at a particular location.

PARCC Sample Item

CCSS: F.BF.3

Identify the effect on the graph of replacing f(x) by f(x)+k, kf(x), f(kx), and f(x+k) for specific values of k (both positive and negative); find the value of k given the graphs. Experiment with cases and illustrate an explanation of the effects on the graph using technology. Include recognizing even and odd functions from their graphs and algebraic expressions for them.

Review from unit assessment:

The figure shows the graphs of the functions y = f(x) and y = g(x). The four indicated points all have integer coordinates.



If $g(x) = k \cdot f(x)$, what is the value of k?



Consider the function f(x), shown in the *xy*-coordinate plane, as the parent function.



Part A

The graph of a transformation of the function f(x) is shown.



Which expression defines the transformation shown?

A. f(x+0)-1 B. f(x+0)+1 C. f(x-1)+0 D. f(x+1)+0

Part B

The graph of a transformation of the function f(x) is shown.



Part C

The graph of a transformation of the function f(x) is shown.



Which expression defines the transformation shown?

- (a) f(x-2) + 0
- $\bigcirc f(x) + 2$
- (b) f(x + 2) + 0

Part D

The graph of a transformation of the function f(x) is shown.



The transformation shown can be expressed in the form y = p[f(x + r)] + n, where *p*, *r*, and *n* are constants. Which value must be less than 0?

p

- ₿ *r*
- © X
- n

Task 2: The function f is defined by $f(x) = x^2 - 2x - 24$. What are the zero(s) of f(x + 3)? Select **all** that apply. (a) x = -7(b) x = -4(c) x = -2(c) x = 0(c) x = 3

 $\bigcirc x = 6$



Task 4:

The graph of the function h(x) is obtained from the graph of f(x) by shrinking the graph of f(x) vertically by a factor of 5 and reflecting the result over the *y*-axis. Which of the following equations gives h(x) in terms of f(x)?

 $\underline{a}. \quad h(x) = 5f(-x)$

$$\mathbf{b}. \quad h(\mathbf{x}) = \frac{1}{5}f(-\mathbf{x})$$

$$\underline{c}. \quad h(x) = -5f(x)$$

$$\underline{d}. \quad h(x) = -\frac{1}{5}f(x)$$



The graph of the function g is shown in the coordinate plane above. If $f(x) = x^2$, and g(x) = k f(x) + c, what are the values of k and c?

- $\underline{a}. \quad k = \frac{1}{3}, \ c = 2$
- $b. \quad k = \frac{1}{3}, \ c = -2$
- c. k = 3, c = 2

 $\underline{d}. \quad k = 3, \ c = -2$



Task 7 Part A

Write an expression that defines f(x + 5).

Enter your expression in the space provided.

Part B

Describe the transformation that maps the graph of f(x) to f(x + 5). Justify your answer algebraically or by using key features of the graphs.

Enter your answer in the space provided.

Task 8

Consider the functions f(x) and g(x) described by the equations and the functions h(x) and k(x) shown by graphs.



Which of the statements are true? Select **all** that apply.

- Is neither an even nor odd function.
- \odot g is an even function.
- \odot g is neither an even nor odd function.
- It is an even function.
- It is an odd function.
- Is an odd function.

CCSS: A. REI.2

Solve simple rational and radical equations in one variable, and give examples showing how extraneous solutions may arise.

Practice

Task 1				
. The table shows the steps and explanations that can be used to solve $\sqrt{x}-5x=-4.$				
			Work	Explanation
			$\sqrt{x} - 5x = -4$	Given
	[Step 1	$\sqrt{x} = 5x - 4$	Addition property of equality
	5	Step 2	$x = 25x^2 - 40x + 16$	Square both sides of the equation
	5	Step 3	$0 = 25x^2 - 41x + 16$	Subtraction property of equality
	5	Step 4	0 = (25x - 16)(x - 1)	Factor
	5	Step 5	(25x - 16) = 0 or (x - 1) = 0	Zero product property
	5	Step 6	25x = 16 or x = 1	Addition property of equality
	5	Step 7	$x = \frac{16}{25}$ or $x = 1$	Division property of equality
Which	step	in the tal	ble could have created an extraneo	us solution?
• A	. Ste	p 1		
© B	. Ste	p 2		
© C	. Ste	p 4		
O D	. Ste	p 5		
	2.0	-		
Task 2	:			
Solve	\sqrt{a}	= a -	6. What is the extraneous solu	ution?
	v			

Algebra II Unit 3 Task 3 What extraneous solution arises when the equation $\sqrt{x+3} = 2x$ is solved for *x* by first squaring both sides of the equation? Task 4 What is the solution to the equation $-\sqrt{x+10} = -7$? Task 5 Solve the equation below. Explain your reasoning for each step. $\sqrt[3]{2x} - 22 = -18$ \

Solve the equation below. Show your work.

$$\sqrt{7x+15} = x+1$$

PARCC Preparation Material -- Solve system of equations

CCSS: A.AREI. 6,

Solve systems of linear equations exactly and approximately (e.g., with graphs), focusing on pairs of linear equations in two variables. (it may contain 3 variables (Solve algebraically a system of three linear equations in three unknowns)

A.APR.7

Solve a simple system consisting of a linear equation and a quadratic equation in two variables algebraically and graphically. For example, find the points of intersection between the line y=-3x and the circle $x^2+y^2=3$.

A.APR.11

Explain why the x-coordinates of the points where the graphs of the equations y=f(x) and y=g(x) intersect are the solutions of the equation f(x)=g(x); find the solutions approximately, e.g., using technology to graph the functions, make tables of values, or find successive approximations. Include cases where f(x) and/or g(x) are linear, polynomial, rational, absolute value, exponential, and logarithmic functions.

PART I

Mini Lesson (Review how to use graphing calculator to solve system..)

Example 1: (calculator allowed question)

 $f(x) = x^2 - 2x - 8$ and $g(x) = \frac{1}{4}x - 1$ What is/are the value(s) of x when g(x) = f(x)

Example 2: (calculator allowed question)

f(x) = |x - 3| and g(x) = 9 - x What are coordinates of the point(s) on the graph when g(x)=f(x)

Practice:

Task 1: (Calculator allowed) Given the functions h(x) = |x - 4| + 1 and $k(x) = x^2 + 3$, which intervals contain a value of x for which h(x) = k(x)? Select all that apply. ® −3 < *x* < −1.5 © −1.5 < *x* < 1.5 ◎ 1.5 < *x* < 3 € 3 < *x* < 4.5 Task 2 (Calculator allowed) $\begin{cases} y = 1 - x^2 \\ y = 2 - x \end{cases}$ How many points of intersection does the given system of equations have? A none ₿ one two C infinitely many D

Task 3 (Calculator allowed)

Functions f and g are defined below.

$$\begin{aligned}
f(x) &= \frac{1}{2x} \\
g(x) &= x^2
\end{aligned}$$

The graphs of y = f(x) and y = g(x) intersect at point *P*.

Determine the *x*-coordinate of *P*. Round your answer to the nearest tenth.

Task 4 (Calculator allowed) Let $f(x) = ax^2$ where a > 0, and let g(x) = mx + b where m > 0 and b < 0. The equation f(x) = g(x) has n distinct real solution(s). What are **all** the possible values of n? Justify your answers. Enter your answers and your justification in the space provided.

Algebra II Unit 3 Task 5 (Calculator allowed) Functions f and g are defined as $f(x) = 2^x$ and g(x) = x + 3. What are the values of x to the nearest hundredth when f(x) = g(x)? Enter your answers in the boxes. $x_1 =$ $x_2 =$

Task 6 (Calculator allowed) Let f(x) = -x + 3 and g(x) = 3 |x| - 1. Where do the graphs of f(x) and g(x) intersect? Enter your answer in the boxes.



Example 1: Solve the system algebraically

$$\begin{cases} y = -x^2 + 5x + 6\\ y = x + 6 \end{cases}$$

Mini lesson/review : (model how to solve a system of three linear equation in TWO variables)

Example 2:

Solve the system

 $\begin{cases} 2y - 3z = 0\\ x + 3y = -4\\ 3x + 4y = 3 \end{cases}$

Example 3: Solve the system

 $\begin{cases} x - 2y + z = -4 \\ -4x + y - 2z = 1 \\ 2x + 2y - z = 10 \end{cases}$

PARCC Practice question



Task 2 (calculator allowed What is the value of z in the solution of the system of linear equations? $\begin{cases}
x - 9y + 4z = 1 \\
-2x + 9y - 4z = -3 \\
2x + y - 4z = -3
\end{cases}$

